# U.S. PATENT APPLICATION

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*Invention:*     **A METHOD AND A SYSTEM RELATED TO DETERMINING THE PRICE OF A COMBINATION CONTRACT**

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# SPECIFICATION

# A METHOD AND A SYSTEM RELATED TO DETERMINING THE PRICE OF A COMBINATION CONTRACT

## TECHNICAL FIELD

The present invention relates to an automated exchange system, and in particular to an automated exchange designed for trading combinations of contracts.

## BACKGROUND OF THE INVENTION AND PRIOR ART

When trading contracts for commodities, financial instruments or the like at an exchange it is quite common that the parties involved in the trade want to trade a number of different contracts all at the same time. Such an order involving a number of simultaneous trades of different products usually is given the precondition that the combined price for all the different subcontracts is equal or better than a predetermined price.

An order involving a number of different simultaneous trades of contracts is usually referred to as a combination order or a combination contract order. For example, a person may wish to buy 7 contracts A and sell 6 contracts B and not pay more than $100 for the whole combination contract. The amount that the person pays or receives when a combination order is traded is referred to the net price of the combination order.

Furthermore, when a combination contract (or a number of them) are to be executed at a given net price, it is often necessary to determine the price for each product/sub-contract of the combination order. The price for each sub-contract, sometimes referred to as a leg, must be set so that when executing all the legs of a combination contract, the total price of all legs will equal the net price of the combination.

However, the prices for the sub-contracts can not be set
arbitrarily. The reason for this is the price structure of
most today existing exchanges. The price for a given contract
is generally traded at a discrete price. In other words it has
to be at a valid price tick, i.e. an integer times the tick
size. Also, there is a restriction that the net price has to
be a valid price tick. For each product at each particular
time, there will also be a valid interval, the price gap
between the best selling price and best buying price
(bid/ask), which is termed the spread.

When trading combination contracts it is always desired and in
some cases required that the price for each sub-contract/leg
is within the spread at the time when the combination order is
traded.

However, today there exist no way of ensuring that all legs
are traded within the spread for each product traded in the
combination contract. The problem arises from the fact that
the sub-contracts are all traded at discrete prices.

Thus, the prices for the individual legs in some cases are
hard to find regardless of which multipliers the legs in the
combination have, regardless of the different spreads,
regardless of the tick size, regardless of the combination
quantity and regardless of the net price at which the
combination order is matched.

Also, the calculations carried out in an automated exchange
system when trying to determine the prices for the individual
legs using a conventional algorithm are extensive, and use
much processor power, and still may fail to deliver prices for
the individual legs that are within the spread.

Today, the solution to this problem is to either let one or more of the legs be traded at a price outside the current spread or to reject the combination order.

Hence, there is a need to find a way to ensure that all combination orders can be traded regardless of which multipliers the legs in the combination contract have, regardless of the different spreads, regardless of the tick size, regardless of the combination quantity and regardless of the net price The algorithm used should preferably also reduce the load on the processor used to make the calculations.

## SUMMARY
It is an object of the present invention to provide an improved computerized trading system for trading combination orders having means for determining the prices for the individual legs regardless of which multipliers the legs in the combination have, regardless of the different spreads, regardless of the tick size, regardless of the combination quantity and regardless of the net price at which orders are matched.

It is another object of the present invention to provide a computerized trading system for trading combination orders that uses less processor power for calculating and determining the prices for the individual legs of a combination order by always providing a solution with a correct net price.

This objects and others are obtained by the present invention as set out in the appended claims. Hence, for each leg, up to two different prices will be selected and allocating the number of products that the multiplier states between the two

prices. Allowing each sub-contract to be traded at, at least, two different price ticks within the spread ensures a solution with a correct net price for each combination contract, which can be repeated any number of times (combination quantity).

## BRIEF DESCRIPTION OF THE DRAWINGS

The present invention will now be described in more detail by way of non-limiting examples and with reference to the accompanying drawings, in which:

- Fig. 1 is a general view of an automated exchange system.
- Fig. 2 is a flow chart illustrating different steps carried out when determining the prices for individual legs in a combination contract.

## DESCRIPTION OF PREFERRED EMBODIMENTS

In Fig. 1, a general view of an automated exchange system is shown. The system comprises a number of remote terminals 10 all connected to a central computer 12 comprising a Central Processing Unit (CPU) 13 and a memory 14 associated therewith. The central computer 12 being loaded with suitable software, such as the CLICK [®] software sold by OM Technology AB, Sweden, forms an automated exchange having all features and functionality of a conventional automated exchange. The remote terminals 10 are designed to send data to and receive data from the central computer 12. The terminals 10 are further designed to provide an interface for investors, such as broker firms etc., trading contracts including combination contracts at the automated exchange.

When trading a combination order in the system shown in Fig. 1, for each leg, up to two different prices can preferably be selected. Further, the number of products that the multiplier states are allocated between the two prices. By allowing the

exchange to use different prices for the same product, a
solution with a correct net price for each combination
contract, which can be repeated any number of times
(combination quantity), can be obtained.

Thus, given a combination contract, a tick size, and a valid
price interval for the product of each leg, there will be a
valid price interval for the net price. If the net price is
outside that interval, it is always impossible to find a valid
solution. Such an order will not be matched in the system.

In Fig. 2, a flow chart illustrating the different steps when
calculating the different prices for the different legs is
shown. The prices are preferably calculated one leg at a time,
and the first leg is initially calculated as indicated in step
201 and 202. Next, in step 203, a percentage is determined
using the net price in relation the combination spread as
input. The percentage is set as the difference between the net
price and the bid price of the current leg divided by the
spread for the current leg.

For the current leg, the percentage determined in step 203 is
applied to the multiplier times the spread of that product,
which gives an optimum price, step 205. Two valid prices are
then selected in a step 207, with one tick apart so that one
is above and one below (or at) the optimum price divided by
the multiplier.

Depending on where the optimum price is compared with the two
selected prices, the number of products given by the
multiplier is allocated between the two prices so that the
average price comes as close as possible to the optimum price,
step 209. When the prices for the first leg are determined,
their contribution is subtracted from the net price, step 210

and the calculations are repeated as indicated in step 211 for
the remaining legs using the residual net price in the
calculations. The procedure is repeated until there are no
more legs in the combination contract and the procedure then
ends in a step 213.

For example, assume that two products, called A and B are
traded at the automated exchange shown in Fig. 1. Assume that
the tick size is 1, i.e. the minimum difference between two
prices. Assume that the spread for A is 4 to 5, i.e. the bid
price is 4 and the ask price is 5 and assume that the spread
for B is 6 to 7. Assume further that a combination order to
buy 5 A and sell 2 B (i.e. one combination contract) is sent
to the exchange.

Thus in this example, the minimum allowed net price is 6
(5*4 - 2*7 = 6) and maximum allowed net price is 13
(5*5 -2*6 = 13). In this example, the net price is set to 9;
i.e. the combination contract is to be traded at the price 9.
If the price for A is selected to 4, the price for B would
have to be 5.50, which cannot be handled, since the tick size
is 1 and which also is outside the spread. The other allowed
price for A is 5, and then the price for B would have to be 8
to give the correct net price, which is outside the spread.

Using the algorithm as described herein the prices for the
individual legs would be 3 contracts A at the price 4 and 2
contracts A at the price 5, and 1 contract B at the price 6
and 1 contract B at the price 7. This gives the correct net
price for each combination contract and it can thus be
multiplied with any combination quantity.

Below an exemplary computer program for implementing the
algorithm described in conjunction with Fig. 2 is shown.

```
// Perform some preparatory calculations
cs_ask[#legs+1] = 0
cs_bid[#legs+1] = 0
loop i: number of legs..1
     if (COMBO.leg[i].operation == BUY)
         c_ask[i] = get_ask_price (COMBO.leg[i].product)
         c_bid[i] = get_bid_price (COMBO.leg[i].product)
     else
         c_ask[i] = -get_bid_price (COMBO.leg[i].product)
         c_bid[i] = -get_ask_price (COMBO.leg[i].product)
     c_ask[i] *= COMBO.leg[i].multipl
     c_bid[i] *= COMBO.leg[i].multipl
     cs_ask[i] = c_ask[i] + cs_ask[i+1]
     cs_bid[i] = c_bid[i] + cs_bid[i+1]
endloop
// cs_bid[1] and cs_ask[1] now contains the allowed spread for the
combo

// Validation of the combo contract is within spread
tmp_net = COMBO.net_price
if (net < cs_bid[1] || tmp_net > cs_ask[1])
     return NOK

loop i: 1..#legs
     percent = (tmp_net-cs_bid[i]) / (cs_ask[i]-cs_bid[i])
     tmp_pri = abs (percent*(c_ask[i]-c_bid[i]) + c_bid[i])
     // Note that the line below should not be performed for the
last
     // leg if the algorithm is modified as described below
     tmp_pri = tick_size * round (tmp_pri/tick_size)
     tmp_pri /= COMBO.leg[i].multipl
     low_pri[i] = tick_size * floor (tmp_pri/tick_size)
     high_pri[i] = l_pri[i] + tick_size
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```
        hpr_vol[i] = (tmp_pri-low_pri[i]) * COMBO.leg[i].multipl /
tick_size
    lpr_vol[i] = COMBO.leg[i].multipl - hpr_vol[i]
    if (COMBO.leg[i].operation == BUY)
        tmp_net -= tmp_pri * COMBO.leg[i].multipl
    else
        tmp_net += tmp_pri * COMBO.leg[i].multipl
endloop
```

Furthermore, it is quite common that the tick size varies over
the whole price interval. This can also be handled by the
algorithm as described herein provided that the combination
tick size is an integer times each tick size. When the two
valid prices are selected one tick apart, it is preferred to
use the tick size that is valid at the optimum price divided
by the multiplier.

Typically; when the tick size varies over the price interval,
the combination tick size will equal the smallest tick size.
Such cases can also be handled by the algorithm as long as all
tick sizes are a multiple of the combination tick size (vice
versa can also be combined). First of all, the legs with non-
zero spread are preferably sorted so that the legs with the
smallest tick size are calculated last. A change in the
algorithm is also required. It should not to round the value
for the last leg (marked in the pseudo code above). Then under
certain circumstances, two selected volumes will in many cases
be non-integers. By converting those to fractional numbers, it
can be determined which combination quantities that will still
yield an integer value for the number of products at each
price. If the smallest tick size equals the combination tick
size, the solution will always be integer values and it will
thus provide a result for any combination quantity. A common
example is that the larger tick size is twice the smaller and

that the combination tick size equals the smaller tick size.
In this case if the net price is an odd number of small ticks
and the tick size for each leg is the larger value, then the
combination quantity must be an even number for the problem to
have a valid solution.

In the examples above, it is assumed that there is a
requirement that all prices determined must be at valid ticks
and within certain interval. If in certain applications such
requirements do not exist, the algorithm can of course still
be used.

If it for some reason is determined that the spread for a
particular leg is zero, that violates one of the initial
assumptions for the algorithm. It can however easily be
treated as well  In that case, the legs only given one valid
price, no spread are calculated first, and assign those legs
the only valid price. Their contribution is then first
subtracted from the net price and the algorithm is then
applied to the remaining legs. If the spread is negative, it
is impossible to assign a valid price at all, and the
combination can thus not be priced.